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Name..... Reg. No.....

# THIRD SEMESTER M.Sc. DEGREE EXAMINATION, NOVEMBER 2020 (CBCSS-PG)

# **CC19P ST3 C11 - APPLIED REGRESSION ANALYSIS**

(Statistics)

(2019 Admission Regular)

Time: Three Hours

Maximum: 30 Weightage

#### Part A

Answer any *four* questions. Each question carries 2 weightage.

- 1. Define multiple linear regression models. What are the assumptions?
- 2. Show that the least square estimate of linear regression model is independent of its residual sum of squares
- 3. What are studentized residuals and PRESS residuals?
- 4. How will you use splines in piecewise polynomial regression modelling?
- 5. What is Serial correlation? How does serial correlation affect regression modeling?
- 6. Explain nonparametric regression model.
- 7. Write a short note on Poisson regression.

## (4 x 2 = 8 Weightage)

### Part B

Answer any *four* questions. Each question carries 3 weightage.

- 8. Let  $Y_1 = \theta + \varepsilon_1$ ,  $Y_2 = 2\theta \varphi + \varepsilon_2$  and  $Y_3 = \theta + 2\varphi + \varepsilon_3$  where  $E(\varepsilon_i) = 0$ , i = 1, 2, 3 and  $\varepsilon_i$ 's are *ii d*. Find the least square estimate of  $\theta$  and  $\varphi$
- 9. Explain bias due to under fitting and bias due to over fitting of a multiple linear regression model.
- 10. What is multicollinearity? Explain the variance decomposition method of detecting multicollinearity and derive the expression for 'Variance Inflation Factor'.
- 11. Discuss the role of dummy variables in linear models. Explain how they are used to indicate different intercepts and different slopes of the regression model. Illustrate with examples.
- 12. What are outliers and high leverage points? Discuss the effect of outliers in regression modelling.
- 13. Explain Mallow's C<sub>P</sub> statistic
- 14. Let  $Y_i$ , i = 1, 2, ..., n be independent random variables and  $Y_i \sim N(i\theta, i^2\sigma^2)$ . Find generalized least square estimator of  $\theta$  (4 x 3 = 12 Weightage)

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### Part C

Answer any *four* questions. Each question carries 5 weightage.

- 15. Obtain the decomposition of the total variation in the data under a multiple linear regression model. Hence, define  $SS_T$ ,  $SS_R$  and  $SS_{Res}$  and indicate the ANOVA.
- 16. Derive the least squares estimators of model parameters for multiple linear regression models. Obtain mean and variance of the estimator.
- 17. Explain the concept of orthogonal polynomials and obtain the first five orthogonal polynomials. Explain how orthogonal polynomials are used in fitting regression models?
- 18. Explain the logistic regression model, interpret the parameters and explain how to test the significance of  $i^{th}$  regressor in a dichotomous logistic model

(2 x 5 = 10 Weightage)

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