19P453	(Pages: 2)	Name:
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# FOURTH SEMESTER M.Sc. DEGREE EXAMINATION, APRIL2021 (CBCSS-PG)

# CC19P MST4 E08 - RELIABILITY MODELING

(Statistics - Elective Course) (2019 Admission - Regular)

Time: Three Hours Maximum: 30 Weightage

#### Part A

Answer any *four* questions. Each question carries 2 weightage.

- 1. Define dual. What is the dual of k out of n system?
- 2. Define minimal path and minimal cut set. How can we represent a coherent system using minimal path and cut expression?
- 3. What are different criteria for identification of IFRA classes of life distribution?
- 4. Distinguish between Type I and Type II censoring.
- 5. What are different types of accelerated life testing procedures?
- 6. What is Availability and limiting availability?
- 7. Define Bivariate exponential distribution. What is the lack of memory property?

 $(4 \times 2 = 8 \text{ Weightage})$ 

## Part B

Answer any *four* questions. Each question carries 3 weightage.

- 8. If  $\varphi(x_1, ..., x_n)$  be the structure function of a coherent system of n components. Show that  $\prod_{i=1}^n x \le \varphi(x_1, ..., x_n) \le \coprod_{i=1}^n x_i$ . Find the corresponding reliability bounds.
- 9. Show that reliability function  $h(\mathbf{P})$ , where  $\mathbf{P} = (p_1, ..., p_n)$  is increasing in  $p_i$ , i = 1, 2, ..., n.
- 10. If  $F_1$  and  $F_2$  are IFR distributions, show that their convolution is also IFR distribution.
- 11. Discuss failure rate property of a Gamma distribution.
- 12. Explain Univariate Poisson shock model if distribution of size of the shock is i.i.d.
- 13. Define reliability importance of components. Obtain the reliability importance of series and parallel system of three components with  $p_1$ =0.2,  $p_2$ =0.2,  $p_3$ =0.3.
- 14. Give failure rate properties of Weibull distribution.

 $(4 \times 3 = 12 \text{ Weightage})$ 

### Part C

Answer any two questions. Each question carries 5 weightage.

15. Show that life distribution is exponential distribution if and only if it has constant failure rate.

- 16. Explain reliability growth testing. Explain the non-parametric estimation of Censored ungrouped data.
- 17. Show that IFRA property of life distributions are preserved under formation of coherent system.
- 18. Explain the testing of homogeneous Poisson process (HPP) Vs non-homogeneous Poisson process (NHPP).

 $(2 \times 5 = 10 \text{ Weightage})$ 

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