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Name: .....

Reg.No:

## THIRD SEMESTER B.Sc. DEGREE EXAMINATION, NOVEMBER 2022

(CBCSS - UG)

(Regular/Supplementary/Improvement)

## CC19U STA3 C03 - PROBABILITY DISTRIBUTIONS AND SAMPLING THEORY

(Statistics - Complementary Course)

(2019 Admission onwards)

Time: 2.00 Hours

Maximum : 60 Marks

Credit : 3

Part A (Short answer questions)

Answer *all* questions. Each question carries 2 marks.

- 1. Find the m.g.f. of a geometric distribution.
- 2. Define Negative binomial distribution.
- 3. Define Exponential distribution.
- 4. What are the mean and variance of Lognormal distribution?
- 5. Describe Cauchy distribution.
- 6. Explain weak law of large numbers.
- 7. State Central limit theorem
- 8. What do you mean by sampling error.
- 9. Define sampling distribution.
- 10. A random sample of size 64 are drawn from a normal population with mean 32 and standard deviation5. Find the mean and variance of sample mean .
- 11. Define student-t statistic.
- 12. Define F statistic.

(Ceiling: 20 Marks)

**Part B** (Short essay questions - Paragraph) Answer *all* questions. Each question carries 5 marks.

- 13. Establish additive property of Binomial distribution.
- 14. Obtain the mgf of Poisson distribution.

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- 15. If X is normally distributed with mean 11 and standard deviation 1.5, find the number  $x_0$  such that (i)  $P(X > x_0) = 0.3$  (ii)  $P(X < x_0) = 0.09$
- 16. For a geometric distribution  $f(x) = 2^{-x}, x = 1, 2, 3...$ , prove that Chebyshev's inequality gives  $P\{|X-2| \le 2\} > \frac{1}{2}$  while the actual probability is  $\frac{15}{16}$ .
- 17. What is systematic sampling?
- 18. Derive the distribution of  $\frac{ns^2}{\sigma^2}$ . Write its p.d.f.
- 19. State the relationship between normal, Chi-square, t anf F distributions.

(Ceiling: 30 Marks)

## Part C (Essay questions)

Answer any one question. The question carries 10 marks.

- 20. State and prove Weak law of large numbers.
- 21. Derive Chi-square distribution with 'n' degrees of freedom.

(1 × 10 = 10 Marks)

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