

## SECOND SEMESTER UG DEGREE EXAMINATION, APRIL 2025

(FYUGP)

## CC24UMAT2CJ101 - INTEGRAL CALCULUS

(Mathematics - Major Course)

(2024 Admission - Regular)

Time: 2.0 Hours

Maximum: 70 Marks

Credit: 4

**Part A** (Short answer questions)Answer **all** questions. Each question carries 3 marks.

1. Suppose that  $\int_1^2 f(x)dx = -4$ ,  $\int_1^5 f(x)dx = 6$ ,  $\int_1^5 g(x)dx = 8$ . Then evaluate [Level:2] [CO1]  
(a)  $\int_1^2 3f(x)dx$ , (b)  $\int_5^1 g(x)dx$ .
2. Evaluate (a)  $\sum_{k=1}^{10} k$  and (b)  $\sum_{k=1}^{10} k^3$ . [Level:2] [CO1]
3. Evaluate  $\int (x^2 - 2x + 5) dx$ . [Level:2] [CO1]
4. Find (a)  $\frac{d}{dx} \ln 2x$  and (b)  $\frac{d}{dx} \ln(x^2 + 3)$ . [Level:2] [CO2]
5. Evaluate  $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{4 \cos \theta}{3 + 2 \sin \theta} d\theta$ . [Level:2] [CO2]
6. Compute  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$  [Level:3] [CO3]
7. Evaluate the integral  $\int \frac{dx}{(x+1)\sqrt{x^2+2x}}$  [Level:3] [CO3]
8. Evaluate the integral  $\int 3\sqrt{\sin v} \cos v dv$  [Level:3] [CO4]
9. Find the area between  $y = \sec^2 x$  and  $y = \sin x$  from 0 to  $\pi/4$ . [Level:2] [CO5]
10. Find the surface area when  $y = 2x$  is revolved about the x-axis from  $x = 0$  to  $x = 3$  [Level:2] [CO5]

**(Ceiling: 24 Marks)****Part B** (Paragraph questions/Problem)Answer **all** questions. Each question carries 6 marks.

11. Evaluate (a)  $\int \sqrt{1+y^2} \cdot 2y dy$  and (b)  $\int x^2 \sin(x^3) dx$  using substitution [Level:3] [CO1]  
method.
12. Find the average value of  $f(x) = x^2 - 1$  on  $[0, \sqrt{3}]$ . At what points on the [Level:2] [CO1]  
given interval does the function assumes its average value?

13. Evaluate (a)  $\int_{-1}^1 3x^2 \sqrt{x^3 + 1} dx$  (b)  $\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \cot \theta \csc^2 \theta d\theta$ . [Level:3] [CO2]
14. Solve the initial value problem  $\frac{dy}{dt} = e^t \sin(e^t - 2)$ ,  $y(\ln 2) = 0$ . [Level:3] [CO2]
15. Using integration by parts compute  $\int_1^2 x \ln x dx$  [Level:3] [CO4]
16. Using method of partial fractions evaluate  $\int \frac{x+4}{x^2+5x-6} dx$  [Level:3] [CO4]
17. Find the length of the curve  $y = \frac{4\sqrt{2}}{3} x^{3/2} - 1$ ,  $0 \leq x \leq 1$  [Level:3] [CO5]
18. Find the volume of the solid generated by revolving the region bounded by  $y = \sqrt{x}$  and the lines  $y = 1$ ,  $x = 4$  about the line  $y = 1$ . [Level:3] [CO5]

**(Ceiling: 36 Marks)**

**Part C (Essay questions)**

Answer any **one** question. The question carries 10 marks.

19. (a) Find the area of the region between the  $x$ -axis and the graph of  $f(x) = x^3 - x^2 - 2x$ ,  $-1 \leq x \leq 2$ . [Level:3] [CO2]
- (b) Express the solution of the following initial value problem as an integral:  
 $\frac{dy}{dx} = \tan x$ ,  $y(1) = 5$ .
20. Find the area of the region in the first quadrant that is bounded above by  $y = \sqrt{x}$  and below by the  $x$ -axis and the line  $y = x - 2$ . [Level:3] [CO5]

**(1 × 10 = 10 Marks)**

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