

|                |  |                              |                       |             |
|----------------|--|------------------------------|-----------------------|-------------|
| Programme      | B. Sc. Mathematics Honours   |                              |                       |             |
| Course Code    | MAT2MN102  |                              |                       |             |
| Course Title   | <b>CALCULUS AND MATRIX ALGEBRA</b>   |                              |                       |             |
| Type of Course | <b>MINOR</b>   |                              |                       |             |
| Semester       | II   |                              |                       |             |
| Academic Level | 100-199  |                              |                       |             |
| Course Details | Credit   | Lecture/Tutorial<br>per week | Practicum<br>per week | Total Hours |
|                | 4  | 4                            | -                     | 60          |
| Pre-requisites | Basic Calculus   |                              |                       |             |
| Course Summary | Students learn about antiderivatives, the indefinite and definite integrals, Riemann sums, and the Fundamental Theorem of Calculus. Course explores the average value of functions, evaluating definite integrals by substitution, calculating areas between curves, and finding the length of plane curves. Next it introduces functions of multiple variables, including notation, graphs, limits, continuity, and partial derivatives for functions of two or more variables. Course also focuses on matrix algebra, determinants, eigenvalue problems (including complex eigenvalues), and orthogonal matrices and their properties. |                              |                       |             |

**Course Outcomes (CO):**

| CO   | CO Statement  | Cognitive Level* | Knowledge Category# | Evaluation Tools used                                 |
|--|---|------------------|---------------------|---|
| CO1  | Demonstrate proficiency in applying calculus techniques to solve analytical and geometrical problems involving indefinite and definite integrals, substitution methods, and integration by parts.   | Ap               | C                   | Internal Exam/Assignment/Seminar/ Viva / End Sem Exam |
| CO2  | Apply multivariable calculus concepts, including functions of multiple variables, limits, continuity, and partial derivatives, to model and analyse real-world phenomena and mathematical problems. | Ap               | C                   | Internal Exam/Assignment/Seminar/ Viva / End Sem Exam |
| CO3  | Apply linear algebra principles, such as matrix operations, determinants, and eigenvalue problems, to analyze and solve systems of equations and geometric problems.                                | Ap               | C                   | Internal Exam/Assignment/Seminar/ Viva / End Sem Exam |
| * - Remember (R), Understand (U), Apply (Ap), Analyse (An), Evaluate (E), Create (C)<br># - Factual Knowledge(F) Conceptual Knowledge (C) Procedural Knowledge (P) Metacognitive Knowledge (M) |   |                  |                     |   |

**Detailed Syllabus:**

|                  |  |   |               |                            |
|------------------|--|---|---------------|----------------------------|
| <b>Text Book</b> | <p>1. <b>Howard Anton, Bivens and Stephen Davis, Calculus- Early Transcendentals (10<sup>th</sup> Edition).</b><br/>                 2. <b>Advanced Engineering Mathematics(6/e): Dennis G Zill Jones &amp; Bartlett, Learning, LLC (2018) ISBN: 9781284105902</b></p> |   |               |                            |
| <b>Module</b>    | <b>Unit</b>  | <b>Content</b>  | <b>Hrs 60</b> | <b>External Marks (70)</b> |
| <b>I</b>         | <b>Indefinite and Definite Integrals</b>   |   | <b>12</b>     | <b>Min 15</b>              |
|                  | 1  | Section 5.2: The Indefinite Integral - Antiderivatives, The Indefinite Integral, Integration Formulas, Properties of the Indefinite Integral, Integral Curves   |               |                            |
|                  | 2  | Section 5.3: Integration by Substitution - u-Substitution, Easy to Recognize Substitutions, Less Apparent Substitutions   |               |                            |
|                  | 3  | Section 5.5: The Definite Integral - Riemann Sums and the Definite Integral, Properties of the Definite Integral.   |               |                            |
|                  | 4  | Section 5.6: The Fundamental Theorem of Calculus - The Fundamental Theorem of Calculus (sub section), The Relationship Between Definite and Indefinite Integrals.   |               |                            |
| <b>II</b>        | <b>Techniques and Applications</b>   |   | <b>13</b>     | <b>Min 15</b>              |
|                  | 5  | Section 5.8: Average Value of a Function and its Applications - Average Value of a Continuous Function (up to and including Example 2 only )  |               |                            |
|                  | 6  | Section 5.9: Evaluating Definite Integrals by Substitution - Two Methods for Making Substitutions in Definite Integrals   |               |                            |
|                  | 7  | Section 6.1: Area Between Two Curves - Area Between $y = f(x)$ and $y = g(x)$ , Reversing the Roles of $x$ and $y$  |               |                            |
|                  | 8  | Section 6.4: Length of a Plane Curve - Arc Length   |               |                            |
|                  | 9  | Section 7.2: Integration by Parts - The Product rule and Integration by Parts, Guidelines for Integration by Parts, Repeated Integration by Parts   |               |                            |
|                  | 10   | Section 7.5: Integrating Rational Functions by Partial Fractions - Partial Fractions, Finding the form of a Partial Fraction Decomposition, Linear Factors, Quadratic Factors (Example 4 is optional), Integrating Improper Rational Functions. |               |                            |
| <b>III</b>       | <b>Multivariable Calculus</b>  |   | <b>10</b>     | <b>Min 15</b>              |
|                  | 11   | Section 13.1: Functions of Two or More Variables: Notation and Terminology, Graphs of Functions of Two Variables.   |               |                            |
|                  | 12   | Section 13.1: Functions of Two or More Variables: Level Curves, Level Surfaces.   |               |                            |
|                  | 13   | Section 13.2: Limits and Continuity - Limit along Curves  |               |                            |
|                  | 14   | Section 13.2: Limits Continuity - Continuity  |               |                            |
|                  | 15   | Section 13.3: Partial Derivatives -   |               |                            |

|                   |                                  |   |           |               |
|-------------------|----------------------------------|---|-----------|---------------|
|                   |                                  | Partial Derivatives of Functions of Two Variables, The Partial Derivative Function, Partial Derivative Notation, Implicit Partial Differentiation, Partial Derivatives and Continuity |           |               |
|                   | 16                               | Section 13.3: Partial Derivatives<br>Partial Derivatives of Functions with more than Two Variables, Higher order Partial Derivatives, Equality of Mixed Partials.                     |           |               |
| <b>IV</b>         | <b>Linear Algebra Essentials</b> |   | <b>13</b> | <b>Min 15</b> |
|                   | 17                               | Section 8.1: Matrix Algebra   |           |               |
|                   | 18                               | Section 8.2: Systems of Linear Algebraic Equations  |           |               |
|                   | 19                               | Section 8.8: The Eigenvalue Problem -<br>Topics up to and including Example 4   |           |               |
|                   | 20                               | Section 8.8: The Eigenvalue Problem -<br>Topics from Complex Eigenvalues onwards  |           |               |
|                   | 21                               | Section 8.10: Orthogonal Matrices -<br>Topics up to and including Theorem 8.10.3  |           |               |
|                   | 22                               | Section 8.10: Orthogonal Matrices -<br>Topics from Constructing an Orthogonal Matrix onwards  |           |               |
| <b>V</b>          | <b>Module V (Open Ended)</b>     |   | <b>12</b> |               |
|                   |                                  | Fundamental theorems in Vector Calculus such as Green's theorem, divergence theorem, and the Stokes' theorem.   |           |               |
|                   |                                  | Trigonometric Substitutions   |           |               |
|                   |                                  | Integrating Trigonometric Functions   |           |               |
|                   |                                  | Volume of Solids of Revolution, Area of Surfaces of Revolution  |           |               |
|                   |                                  | The Chain Rule in Partial Differentiation   |           |               |
|                   |                                  | Directional Derivatives and Gradients, Tangent Planes and Normal Vectors  |           |               |
|                   |                                  | Basics of Vector Calculus including the differential operators such as gradient, divergence and curl.   |           |               |
|                   |                                  | Simpsons Rule, Trapezoidal rule in Numerical Integration  |           |               |
|                   | Algebra of Complex Numbers       |   |           |               |
| <b>References</b> |                                  |   |           |               |
|                   | 1                                | Calculus and Analytic Geometry, 9 th Edition, George B. Thomas Jr and Ross L. Finney, Pearson Publications.   |           |               |
|                   | 2                                | Calculus, Soo T. Tan, Brooks/Cole Cengage Learning (2010) ISBN-13: 978-0-534-46579-7.   |           |               |
|                   | 3                                | Marsden, Jerrold, and Alan Weinstein. <i>Calculus I</i> . Springer Science & Business Media, 1985.  |           |               |
|                   | 4                                | Stein, Sherman K. <i>Calculus in the first three dimensions</i> . Courier Dover Publications, 2016.   |           |               |
|                   | 5                                | Kreyszig, Erwin. <i>Advanced Engineering Mathematics 9th Edition with Wiley Plus Set</i> . Vol. 334. US: John Wiley & Sons, 2007.   |           |               |
|                   | 6                                | Elementary Linear Algebra, Applications version, 9 th edition, Howard Anton and Chriss Korres   |           |               |

**Note: 1) Optional topics are exempted for end semester examination. 2) Proofs of all the results are also exempted for the end semester exam.**

**Mapping of COs with PSOs and POs :**

|      | PSO5 | PSO6 | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 |
|------|------|------|-----|-----|-----|-----|-----|-----|-----|
| CO 1 | 2    | 1    | 3   | 1   | 1   | 1   | 3   | 0   | 0   |
| CO 2 | 2    | 1    | 2   | 1   | 2   | 1   | 2   | 0   | 0   |
| CO 3 | 2    | 1    | 2   | 1   | 2   | 1   | 2   | 0   | 0   |

**Correlation Levels:**

| Level | Correlation        |
|-------|--------------------|
| -     | Nil                |
| 1     | Slightly / Low     |
| 2     | Moderate / Medium  |
| 3     | Substantial / High |

**Assessment Rubrics:**

- Assignment/ Seminar
- Internal Exam
- Viva
- Final Exam (70%)

**Mapping of COs to Assessment Rubrics:**

|      | Internal Exam | Assignment | Seminar | Viva | End Semester Examinations |
|------|---------------|------------|---------|------|---------------------------|
| CO 1 | ✓             | ✓          | ✓       | ✓    | ✓                         |
| CO 2 | ✓             | ✓          | ✓       | ✓    | ✓                         |
| CO 3 | ✓             | ✓          | ✓       | ✓    | ✓                         |