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# THIRD SEMESTER M.Sc. DEGREE EXAMINATION, NOVEMBER 2022 (CBCSS - PG) 

(Regular/Supplementary/Improvement)

## CC19P CSS3 E01f - NUMERICAL AND STATISTICAL METHODS

(Computer Science)
(2019 Admission onwards)
Time : 3 Hours
Maximum : 30 Weightage

## Part-A

Answer any four questions. Each question carries 2 weightage.

1. Explain errors and their types.
2. Apply Gauss Siedel method to solve the equations : $20 \mathrm{x}+\mathrm{y}-2 \mathrm{z}=17$,

$$
\begin{aligned}
& 3 x+20 y-z=-18 \\
& 2 x-3 y+20 z=25
\end{aligned}
$$

3. Calculate $\int_{1}^{1.4} e^{-x^{2}} d x$ using trapezoidal rule, considering four equal parts.
4. Calculate $\int_{0}^{6} \frac{1}{1+x^{2}} \mathrm{dx}$ using Simpson's $1 / 3$ rule.
5. If $\mathrm{P}(\mathrm{A})=1 / 4, \mathrm{P}(\mathrm{B})=1 / 3$ and $\mathrm{P}(\mathrm{A} \cup \mathrm{B})=1 / 2$. Find the values (a) $\mathrm{P}(\mathrm{A} \cap \mathrm{B})$
(b) $\mathrm{P}\left(\mathrm{A} \cap \mathrm{B}^{\prime}\right)$
(c) $P\left(A^{\prime} \cap B^{\prime}\right)$
6. State and Prove the multiplication theorem for two independent events.
7. There are two bags, one containing 5 white and 4 black balls and the other containing 6 white and 5 back balls. One bag is chosen and one ball is drawn. If it is white, what is the probability that the bag selected is the first.

$$
(4 \times 2=8 \text { Weightage })
$$

## Part-B

Answer any four questions. Each question carries 3 weightage.
8. Find the real root of the equation $f(x)=2 x-\log x-6$, by the method of regula- falsi position correct to 3 decimal places.
9. Find the root of the equation $2 x-\log x=7$, using secant method to 5 decimal places.
10. Find the cubic polynomial which takes the following values using Newton's forward difference method:

| x | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| y | 1 | 2 | 1 | 10 |

11. Calculate using Runge-kutta fourth order $y(0.1)$, given $\frac{d y}{d x}=x+y, y(0) 1$.
12. An article manufactured by a company consists of two parts A and B . In the process of manufacturing part A, 9 out of 100 are likely to be defective. Similarly, 5 out of 100 are likely to be defective in the manufacture of part B. Calculate the probability that the assembled part will not be defective.
13. A continuous random variable x has the following density function

$$
\begin{aligned}
f(x) & =a x, 0 \leq x \leq 1 \\
& =a, 1<x \leq 2 \\
& =-a x+3 a, 2<x \leq 3
\end{aligned}
$$

14. Solve the following Transportation problem using Vogel's Approximation method to minimize the total cost of transportation.

|  | Destination 1 | Destination 2 | Destination 3 | Destination 4 | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Source1 | 14 | 56 | 48 | 27 | 70 |
| Source2 | 82 | 35 | 21 | 81 | 47 |
| Source3 | 99 | 31 | 71 | 63 | 93 |
| Supply | 70 | 35 | 45 | 60 |  |

( $4 \times 3=12$ Weightage)

## Part-C

Answer any two questions. Each question carries 5 weightage.
15. Apply Gauss elimination method to solve the equations: $x+4 y-z=-5$,

$$
\begin{gathered}
x+y-6 z=-12 \\
3 x-y+z=-5
\end{gathered}
$$

16. Find the value at $\mathrm{x}=4$ using Lagrange's formula

| $x$ | 1.5 | 3 | 6 |
| :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ | -0.25 | 2 | 20 |

17. A factory uses 3 different resources for manufacturing 2 different products. 20 units of the resources A, 12 units of resource $B$ and 16 units of resource $C$ being available. One unit of first product requires 2,2 and 4 with unit respective resources and one unit of the second product requires 4,2 and 0 units of the respective resources . Given that the first product gives a profit of Rs. 2/- per unit and second Rs. 3/-. Formulate the linear programming problem. How many units of each product should be produced to maximize the profit? Solve it graphically.
18. A company has 4 machines(M1,M2,M3 and M4) to do 3 jobs( $\mathrm{J} 1, \mathrm{~J} 2$ and J 3 ) . Each job can be assigned to one and only one machine. The cost of each job on each machine is given in the following table. What are the job assignments which will minimize the cost?

|  | M1 | M2 | M3 | M4 |
| :---: | :---: | :---: | :---: | :---: |
| J1 | 18 | 24 | 28 | 32 |
| J2 | 8 | 13 | 17 | 19 |
| J3 | 10 | 15 | 19 | 24 |

