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SECOND SEMESTER M.Sc. DEGREE EXAMINATION, MAY 2018

(Regular/Supplementary/Improvement)

(CUCSS - PG)

(Statistics)

CC15P ST2 C09 - DESIGN AND ANALYSIS OF EXPERIMENTS

(2015 Admission onwards)

Time: Three Hours

Maximum: 36 Weightage

PART A

Answer *all* questions. Each question carries 1 weightage.

- 1. Define linear hypothesis.
- 2. Explain the role of local control in design of experiments.
- 3. Write a short note on model adequacy checking.
- 4. Give an example of a Graeco Latin square design.
- 5. Write a short note on efficiency of Latin square designs.
- 6. Distinguish between orthogonal and non-orthogonal data.
- 7. Define Partially Balanced Incomplete Block Design with two associate classes.
- 8. State four parametric relations in BIBD.
- 9. State the connection of Youden square with Latin square design.
- 10. Explain the concept of blocking in a factorial design.
- 11. Obtain the main effects and interaction effects of a 2^2 factorial design.
- 12. Write a short note on split plot designs.

(12 x 1 = 12 Weightage)

PART B

Answer any *eight* questions. Each question carries 2 weightage.

- 13. Discuss the regression approach to the analysis of variance.
- 14. State and prove a necessary and sufficient condition for the estimability of a parametric function.
- 15. Let the model equation be $y_1 = 2\alpha_1 + 3\alpha_2 + e_1$, $y_2 = 3\alpha_1 + 4\alpha_2 + e_2$, $y_3 = 4\alpha_1 + 5\alpha_2 + e_3$. Find the best estimates of α_1 and α_2 .
- 16. Derive the expression for the expected value of mean squares in RBD.

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- 17. Derive the analysis of Latin Square Design.
- 18. If a single observation is missing in Randomized Block Design, estimate the missing value.
- 19. Construct a Balanced Incomplete Block Design with v = 16, b = 20, k = 4, r = 5 and $\lambda = 1$.
- 20. Write a short note on inter block analysis of Balanced Incomplete Block Design.
- 21. Explain how different blocks in Lattice Design are formed.
- 22. Distinguish between symmetrical and asymmetrical factorial experiments. Give an example for each.
- 23. Construct a $\frac{1}{4}$ replicate of a 2⁶ factorial design. Give the aliases of main effects and two

factor interactions.

24. Describe the analysis of a 3^2 factorial design.

(8 x 2 = 16 Weightage)

PART C

Answer any two questions. Each question carries 4 weightage.

- 25. For the model $y_1 = \theta_1 + \theta_2 + e_1$, $y_2 = \theta_1 + \theta_3 + e_2$, $y_3 = \theta_1 + \theta_2 + e_3$, show that $c_1\theta_1 + c_2\theta_2 + c_3\theta_3$ is estimable if $c_1 = c_2 + c_3$. Obtain the best estimate of $\theta_1 + 2\theta_2 \theta_3$ if e_i are independent $N(0, \sigma^2)$ variables. What is the variance of the estimate?
- 26. Develop the analysis of covariance for Randomized Block Design with one concomitant variable stating clearly the assumptions.
- 27. What is meant by Balanced Incomplete Block Design? In a BIBD prove that the number of blocks can never be less than the number of treatments.
- 28. A 2^4 factorial experiment is conducted in Randomized Block Design. The block size is 8 and the effect confounded is ABCD. Describe the analysis if it is replicated 4 times.

(2 x 4 = 8 Weightage)
