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# FOURTH SEMESTER M.Sc. DEGREE EXAMINATION, MARCH 2017 (CUCSS - PG)

(Statistics)

## CC15P ST4 C13-MULTIVARIATE ANALYSIS

(2015 Admission) embession and established and extended the second subsect and analysis of

Time: 3 Hours Maximum: 36 Weightage

### 22. If $X \sim N(\mu, \Sigma)$ and $\Sigma$ is non-singular **A traq** ive the distribution of $(X - \mu)^{*} \Sigma^{*}(X - \mu)$ .

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- 1. Define singular multivariate normal distribution.
- 2. What do you mean by generalized variance?
- 3. Define multiple correlation coefficient
  - 4. Show that every linear combination of a set of random variables is normal, then their joint distribution is also normal.
  - 5. What is Fisher-Behren problem?
  - 6. Define partial correlation coefficient.
  - 7. Describe multivariate classification problem in the first the more distributed and several 25
  - 8. Explain sphericity test.
  - 9. Discuss the relationship connecting  $T^2$  and  $D^2$ .
  - 10. What are canonical correlation coefficient and canonical variables?
  - 11. What is factor analysis? Is a seed on one meldon not applied by editored TS
  - 12. Justify the statement Principal Component Analysis is a data reduction technique.

(12x1=12 Weightage)

#### Part B

Answer any eight questions

- 13. Obtain the characteristic function of a multivariate normal distribution.
- 14. Obtain the MLE of  $\mu$  and  $\Sigma$  in N( $\mu$ ,  $\Sigma$ ).
- 15. Derive the density of a p-variate normal distribution.
- 16. Prove that for a *p*-variate normal distribution, the sample mean vector and variance covariance matrix are independently distributed

- 17. If  $X \sim N(\mu, \Sigma)$ , State and prove the necessary and sufficient condition for the independence of two quadratic forms X'A X and X'BX.
- 18. If  $X = [X^{(1)}, X^{(2)}]' \sim N(\mu, \Sigma)$ . Derive the conditional distribution of  $X^{(1)}$  given  $X^{(2)}$ .
- 19. Obtain the null distribution of sample correlation.
- 20. Explain the testing procedure for independence of sets of variates of *p*-variate normal distribution
- 21. Discuss any two properties of Wishart distribution.
- 22. If  $X \sim N(\mu, \Sigma)$  and  $\Sigma$  is non-singular then derive the distribution of  $(X-\mu)' \Sigma^{-1}(X-\mu)$ .
- 23. How will you test for the population mean of a *p*-variate normal distribution when the dispersion matrix is known?
- 24. Discuss Baye's classification problem

(8x2=16 Weightage)

#### Part C

Answer any two questions

- 25. Derive the distribution of Hotelling's  $T^2$ -Statistic in the null case furn edipsed.
- 26. Establish that  $T^2$  is invariant under linear transformation. Also derive the use of  $T^2$  statistic in testing equality of means of two multivariate normal populations having equal covariance matrices.
- 27. Describe the classification problem into one of several populations part at and W. [1]
- 28. Establish the relationship between principal component & eigen structure of the variance. correlation matrices.

(2x4=8 Weightage)

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3. Obtain the characteristic function of a multivariate normal distribution

15. Derive the density of a p-variate normal distribution.

16. Prove that for a p-variate normal distribution, the sample mean vector and variance