19P156

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Name: ..... Reg. No.....

### FIRST SEMESTER M.Sc. DEGREE EXAMINATION, NOVEMBER 2019 (CUCSS PG) CC19P MST1 C01 – ANALYTICAL TOOLS FOR STATISTICS – I

(Statistics)

(2019 Admission Regular)

Time: Three Hours

Maximum: 30 Weightage

#### PART A

Answer any *four* questions. Each question carries 2 weightage.

- 1. Verify the Cauchy-Reimann equations of the complex function  $f(z) = \frac{\overline{z}}{|z|^2}$
- 2. Show that the real and imaginary parts of the analytic function satisfies Laplace equation.
- 3. Find the complex function where the real part is given by

 $u_x = e^x(\cos(y) - y\sin(y))$  given that the function is analytic.

- 4. Evaluate  $\int_C Z^2 dz$  where C the straight line is joining the origin to the point.
- 5. State and prove Cauchy's integral formula.
- 6. Find

a). 
$$\int_C \frac{3Z^2 + 7Z + 1}{Z + 1} dz$$
, where  $C: |Z + 1| = 1$   
b).  $\int_C \frac{5Z - 2}{Z(Z - 1)} dz$ , where  $C: |Z| = 2$ 

7. Show that  $\lim_{(x,y)\to(0,0)} f(x,y)$  does not exist, where  $f(x,y) = \begin{cases} \frac{x^2 - y^2}{x^2 + y^2}, & (x,y) \neq 0\\ 0, & (x,y) = 0 \end{cases}$ 

## (4 x 2 = 8 Weightage)

#### PART B

Answer any *four* questions. Each question carries 3 weightage.

8. Explain the method of Lagrangian multiplier.

9. Find the inverse Laplace transform of  $\frac{2s+7}{3s^2+5}$  and  $\frac{1}{s(1+2s)}$ 

- 10. Derive the polar form of Cauchy Reimann equations.
- 11. Find the Taylor series expansion of

a). 
$$\frac{1}{Z^2 - 3Z + 2}$$
 in  $0 < |Z| < 1$  b).  $\frac{5Z + 7}{(Z + 2)(Z + 3)}$  in  $|Z| < 2$ 

12. Find the Fourier transform of  $f(x) = e^{-|x|}, -\infty < x < \infty$ 

- 13. State and prove Laurent's theorem.
- 14. Find the Laplace transform of the following functions:

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a) t sin(\beta t)
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b) cos(*at*)

c)  $te^t + \cosh(t)$ 

(4 x 3 = 12 Weightage)

# PART C

Answer any *two* questions. Each question carries 5 weightage.

15. Solve the initial value problem using Laplace transform

$$y'' - y' - 6y = 0$$
,  $y(0) = 6$ ,  $y'(0) = 13$ .

16. Evaluate  $\int_0^{\pi} \frac{d\theta}{1 + \cos(\theta)}$ 

17. State and prove Poisson's Integral formula.

18. Find the Fourier series corresponding to the function

$$f(x) = \begin{cases} -k, & when -\pi < x < 0 \\ k, & when 0 < x < \pi \end{cases} \text{ and } f(x + 2\pi) = f(x).$$

(2 x 5 = 10 Weightage)

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