

22U522S

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Name: .....

Reg. No: .....

**FIFTH SEMESTER B.Voc. DEGREE EXAMINATION, NOVEMBER 2024**

(Supplementary)

**CC18U GEC5 OT15 – NUMERICAL ANALYSIS AND OPTIMIZATION TECHNIQUES**

(Information Technology – Common Course)

(2018 to 2020 Admissions)

Time: Three Hours

Maximum: 80 Marks

**PART A**

Answer *all* questions. Each question carries 1 mark.

1. What do you mean by fixed point system? Give an example.
2. What is Percentage error?
3. Write Newton – Raphson formula
4. What is algebraic equation? Give an example.
5. Using bisection method find first two iterations of  $x^3 - x - 1 = 0$
6. Give an equation connecting E and  $\Delta$
7. Write Newton's forward interpolation formula
8. Define average operator  $\mu$
9. Define Surplus variable
10. What is an optimal solution?

**(10 × 1 = 10 Marks)**

**PART B**

Answer any *eight* questions. Each question carries 2 marks.

11. Explain rates of convergence in numerical methods with an example
12. Explain Round off error and Absolute error
13. Prove that  $\Delta = E\mu$
14. Construct Newton's backward difference table  
X : 10 20 30 40  
Y : 1.1 2 4.4 7.9
15. Using method of false position solve the equation  $\cos x = 3x - 1$
16. Using Trapezoidal Rule evaluate  $\int_1^2 x dx$  considering 4 subintervals
17. Find f(2) using Lagrange's interpolation formula  
X : 0 1 3 4  
Y : -12 0 12 24

(1)

**Turn Over**

18. What is interpolation formula?  
 19. Explain assignment problem  
 20. Using Picard's method Solve  $\frac{dy}{dx} = x + y$   $Y(0) = -1$   
 21. Find the dual of the following L.P.P  
 Minimise  $Z = 2x_1 + 9x_2 + x_3$   
 Subject to  $x_1 + 4x_2 + 2x_3 > 5$   
 $3x_1 + x_2 + 2x_3 > 4$   
 $x_1, x_2, x_3 \geq 0$

22. Obtain initial basic feasible solution for the transportation problem.

		To				
		D	E	F	G	
From	A	11	13	17	14	250
	B	16	18	14	10	300
	C	21	24	13	10	400
		200	225	275	250	

(8 × 2 = 16 Marks)

**PART C**

Answer any six questions. Each question carries 4 marks.

23. Gauss Seidel method solve the equations  
 $5x + 2y + z = 12$   
 $X + 4y + 2z = 15$   
 $x + 2y + 5z = 20$
24. Using Sterling's formula find  $f(1.22)$   
 X: 1    1.1    1.2    1.3    1.4  
 Y: 0.841    0.891    0.932    0.963    0.985
25. Using Simpson's rules estimate the integral  $\int_{-1}^1 1 + x^2 dx$
26. Find  $Y(1.1)$  using Taylor's series method  $\frac{dy}{dx} = x + Y$ ,  $y = 1$  when  $x = 0$
27. Find  $f^I(1)$  and  $f^{II}(1)$   
 X : 1    1.05    1.10    1.15    1.20    1.25    1.30  
 Y : 1    1.0247    1.0488    1.0723    1.0954    1.1180    1.1401
28. Explain assignment problem

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29. Solve the following L.P.P

Maximise  $Z = 3x_1 + 9x_2$   
 Subject to  $x_1 + 4x_2 \leq 8$   
 $x_1 + 2x_2 \leq 4$   
 $x_1, x_2 \geq 0$

30. Explain dual simplex method.  
 31. Write a short note on Travelling salesman problem.

(6 × 4 = 24 Marks)

**PART D**

Answer any two questions. Each question carries 15 marks.

32. Using Croute's triangularization method solve the equations.

$x_1 - x_2 + x_3 = 1$   
 $-3x_1 + 2x_2 - 3x_3 = -6$   
 $2x_1 - 5x_2 + 4x_3 = 5$

33. Use fourth Runge-kutta method to find the value of  $y(0.2)$  and  $y(0.4)$  given that

$\frac{dy}{dx} = x^2 + y^2$   $y(0) = 1$  And  $h = 0.1$

34. Using Newton's divided difference formula find  $f(2)$

X	:	5	7	11	13	17
Y	:	150	392	1452	2366	5202

35. Find the solution of  $\frac{dy}{dx} = y(x + y)$ ,  $Y(0) = 1$  using Millen's predictor corrector formula.

Given  $Y(0.1) = 1.11689$ ,  $Y(0.2) = 1.27739$  and  $Y(0.3) = 1.50412$

(2 × 15 = 30 Marks)

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