

29. Solve by dual-simplex method

Maximize $z = 2x_1 + x_2$
 Subject to the constraints $x_1 + 2x_2 \leq 10$;
 $x_1 + x_2 \leq 6$;
 $x_1 - x_2 \leq 2$;
 $x_1 - 2x_2 \leq 1$;
 $x_1 \geq 0, x_2 \geq 0$.

30. Solve the transportation problem.

	D_1	D_2	D_3	D_4	Supply
O_1	3	7	6	4	5
O_2	2	4	3	2	2
O_3	4	3	8	5	3
Demand	3	3	2	2	

31. (a) Explain the Traveling Salesman Problem.

(b) Solve the following Traveling Salesman Problem so as to minimize the cost per cycle.

Jobs	To				
	A	B	C	D	E
A	-	3	6	2	3
B	3	-	5	2	3
C	6	5	-	6	4
D	2	2	6	-	6
E	3	3	4	6	-

32. A small project consists of seven activities for which the relevant data are as given below:

Activity	Preceding Activities	Activity Duration(Days)
A	-	4
B	-	7
C	-	6
D	A, B	5
E	A, B	7
F	C, D, E	6
G	C, D, E	5

- Draw the network and find the project completion time.
- Calculate total float for each of the activities.
- Draw the time scaled diagram.

(3 x 10= 30 Marks)

(4)

18U204

(Pages: 4)

Name.....

Reg. No.....

SECOND SEMESTER B.C.A. DEGREE EXAMINATION, APRIL 2019

(CUCBCSS – UG)

CC17U BCA2 C04 – OPERATIONS RESEARCH

Mathematics – Complementary course

(2017 Admission onwards)

Time: Three Hours

Maximum: 80 Marks

PART A

Answer *all* questions. Each question carries 1 mark.

- Define slack and surplus variables in a Linear Programming Problem.
- Define basic feasible solution of a Linear Programming Problem.
- What do you understand about artificial variable in an LPP?
- What is the necessary and sufficient condition for the existence of the feasible solution of the general transportation problem?
- What do you understand about loop in transportation problem?
- What is transshipment problem?
- How do you convert a maximization assignment problem to minimization problem?
- Define critical path of a Network.
- What is idle time on a machine?
- What is no passing rule in sequencing problem?

(10 x 1= 10 Marks)

PART B

Answer *all* questions. Each question carries 2 marks.

11. Write the following LPP to standard form

$$\text{Maximize } Z = 3x_1 - 3x_2$$

$$\text{subject to } x_1 - 2x_2 \leq -3;$$

$$4x_1 + x_2 \leq 4;$$

$$x_1, x_2 \geq 0$$

- Explain the two-phase method to solve a Linear Programming Problem.
- Is the number of constraints in the primal and dual problems same? Justify.
- Write algorithm for Vogel's Approximation Method to obtain an initial basic feasible solution of the transportation problem.
- How does the problem of degeneracy arise in a transportation problem? Explain how does one overcome it?
- Give the mathematical formulation of an assignment problem.

(1)

Turn Over

17. Write the following assignment problem as a transportation problem.

	A_1	A_2	A_3
R_1	1	2	3
R_2	4	5	1
R_3	2	1	4

18. What is meant by graphing in Network Analysis?

(8 x 2 = 16 Marks)

PART C

Answer any *six* questions. Each question carries 4 marks.

19. A company sells two different products A and B. The company makes a profit of Rs. 40 and Rs. 30 per units on products A and B respectively. The two products are produced in a common production process and are sold in two different markets. The production process has a capacity of 30000 man hours. It takes 2 hours to produce one unit A and *one hour* to produce one unit B. The market has been surveyed, and the company officials feels that the maximum number of units of A that can be sold is 8000 and the maximum units of B is 12000 units. Subject to these limitations, the product can be sold in any convex combination. Formulate this problem as a LP Problem.

20. Find all basic solutions to the system of linear equations $x_1 + 2x_2 + x_3 = 4$;

$2x_1 + x_2 + 5x_3 = 5$, Are the solutions degenerate.

21. Use simplex method to solve the LPP:

Maximize $Z = 3x_1 + 2x_2$

Subject to $4x_1 + 3x_2 \leq 12$

$4x_1 + x_2 \leq 8$

$4x_1 - x_2 \leq 8$

$x_1, x_2 \geq 0$

22. Use Big M- method to solve:

Maximize $z = -x_1 - x_2 - x_3$

Subject to the constraints $x_1 - x_2 - 2x_3 = 2$

$x_1 + 2x_2 - x_3 = 1$

$x_1, x_2, x_3 \geq 0$

23. Using North West Corner Rule find the initial basic feasible solution of

	D_1	D_2	D_3	Availability
O_1	3	2	5	6
O_2	9	1	2	10
O_3	4	3	1	12
Requirments	9	16	3	

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24. Obtain an initial basic feasible solution to the following transportation problem by matrix minima method.

	D_1	D_2	D_3	D_4	Capacity
O_1	1	2	3	4	6
O_2	4	3	2	0	8
O_3	0	2	2	1	10
Demand	4	6	8	6	

25. Consider the problem of assigning five jobs to five persons. The assignment costs are given as follows. Determine the optimum assignment schedule.

Persons		Job				
		1	2	3	4	5
	A	8	4	2	6	1
	B	0	9	5	5	4
	C	3	8	9	2	6
	D	4	3	1	0	3
E	9	5	8	9	5	

26. Distinguish between PERT and CPM in network analysis.

27. Use graphic method to find the minimum elapsed total time sequence of 2 jobs and 5 machines, when we are given the following information:

Job 1	{	Sequence	A	B	C	D	E
	}	Time (in hours)	2	3	4	6	2
Job 2	{	Sequence	C	A	D	E	B
	}	Time (in hours)	4	5	3	2	6

(6 x 4= 24 Marks)

PART D

Answer any *three* questions. Each question carries 10 marks.

28. Use simplex method to solve,

Minimize $z = x_1 - 3x_2 + 2x_3$

Subject to $3x_1 - x_2 + 2x_3 \leq 7$;

$-2x_1 + 4x_2 \leq 12$;

$-4x_1 + 3x_2 + 8x_3 \leq 10$;

$x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$.

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Turn Over