

16U603

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Name: .....

Reg. No.....

**SIXTH SEMESTER B.Sc. DEGREE EXAMINATION, APRIL 2019**

(Regular/Supplementary/Improvement)

(CUCBCSS-UG)

**CC15U MAT6 B11 - NUMERICAL METHODS**

Mathematics - Core Course

(2015 Admission onwards)

Time: Three Hours

Maximum: 120 Marks

**Part-A**

Answer *all* questions. Each question carries 1 mark.

1. Give an example of transcendental equation.
2. Write Newton - Raphson formula for the approximate root of transcendental equation.
3. Find  $\Delta^2 x$
4. Define the mean operator  $\mu$
5. Define the central difference operator  $\delta$
6. Define interpolation.
7. Write the relation between the forward difference operator  $\Delta$  and differential operator  $D$ .
8. By Simpson's  $\frac{1}{3}$ -rule  $\int_{x_0}^{x_n} y dx = \dots$
9. Write the Trapezoidal rule for numerical integration.
10. Define the characteristic equation of a square matrix  $A$
11. Define spectrum of a square matrix.
12. Write the second order Runge-Kutta formula.

(12 × 1 = 12 Marks)

**Part-B**

Answer any *ten* questions. Each question carries 4 marks.

13. Explain Bisection Method.
14. Find a real root of  $x^3 - x - 4 = 0$  by the method of false position.
15. Prove that  $\nabla E = \delta E^{\frac{1}{2}}$
16. Given  $u_x = e^{ax+b}$ , then find  $\Delta^n u_x$
17. Prove that  $\mu^2 = 1 + \left(\frac{1}{4}\right) \delta^2$
18. Draw the table for Gauss Central difference backward formula.
19. Prove that the divided difference of a constant is zero.
20. Prove that the divided differences are symmetric functions of their arguments.
21. Use Simpsons  $\frac{3}{8}$  Rule, find  $\int_{1.6}^{2.2} y dx$  from the table

|   |       |      |       |       |
|---|-------|------|-------|-------|
| x | 1.6   | 1.8  | 2     | 2.2   |
| y | 4.953 | 6.05 | 7.389 | 9.025 |

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**Turn Over**

22. Find the Eigen values of the matrix  $\begin{bmatrix} 2 & 4 \\ 0 & 1 \end{bmatrix}$
23. Decompose the matrix  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$  in to the form  $LU$ , where  $L$  is the lower triangular matrix and  $U$  is an upper triangular matrix.
24. Find  $y(0.01)$  by Euler's method, given that  $y' = xy$  and  $y(0) = 1$
25. Find the first approximation for  $y$  from the differential equation  $y' = x + y$  with  $y(0) = 1$ , using Picard's method.
26. Give the predictor-corrector formula by Adams-Moulton method.

(10 × 4 = 40 Marks)

**Part-C**

Answer any *six* questions. Each question carries 7 marks.

27. Find the smallest root of the equation  $x^3 - 6x^2 + 11x - 6 = 0$ , using Ramanujan's Method.
28. Solve by Secant method to find a real root of  $x^3 - 2x - 5 = 0$
29. Find the value of  $y(0.05)$  from the following table using Newton's forward difference interpolation formula

|   |   |        |        |        |        |
|---|---|--------|--------|--------|--------|
| x | 0 | 0.1    | 0.2    | 0.3    | 0.4    |
| y | 1 | 1.2214 | 1.4918 | 1.8221 | 2.2255 |

30. Use Lagrange formula to find a cubic polynomial which approximate the following data

|   |     |    |   |   |
|---|-----|----|---|---|
| x | -2  | -1 | 2 | 3 |
| y | -12 | -8 | 3 | 5 |

31. Find  $x$  for  $\sinh x = 62$  from the table

|               |         |         |         |         |         |
|---------------|---------|---------|---------|---------|---------|
| $x$           | 4.80    | 4.81    | 4.82    | 4.83    | 4.84    |
| $y = \sinh x$ | 60.7511 | 61.3617 | 61.9785 | 62.6015 | 63.2317 |

32. Find  $\frac{dy}{dx}$  at  $x = 1$  and at  $x = 3$  from the computed table

|     |        |        |        |        |       |        |        |
|-----|--------|--------|--------|--------|-------|--------|--------|
| $x$ | 0      | 1      | 2      | 3      | 4     | 5      | 6      |
| $y$ | 6.9897 | 7.4036 | 7.7815 | 8.1291 | 8.451 | 8.7506 | 9.0309 |

33. Solve using Gauss elimination method

$$\begin{aligned} x + y + z &= 9 \\ 2x - 3y + 4z &= 13 \\ 3x + 4y + 5z &= 40 \end{aligned}$$

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34. Find the inverse of the matrix  $\begin{bmatrix} 4 & -1 & 2 \\ -1 & 2 & 3 \\ 5 & -7 & 9 \end{bmatrix}$  by  $LU$  decomposition method.

35. Using 4<sup>th</sup> order Runge-Kutta method evaluate  $y(0.2)$  and  $y(0.4)$  where  $\frac{dy}{dx} = 1 + y^2$  and  $y(0) = 0$

(6 × 7 = 42 Marks)

**Part- D**

Answer any *two* questions. Each question carries 13 marks.

36. (a) Find a double root of  $f(x) = x^3 - 7x^2 + 16x - 12$  by using generalized Newton's method with  $x = 1.5$
- (b) Solve the equation  $x^3 - 9x + 1$  for the root lying between 2 and 3, correct to 3-significant figures.
37. From the following table find the number of students who obtained marks between 60 and 70 using Gauss backward interpolation formula

| Marks   | No of Students |
|---------|----------------|
| 0-40    | 250            |
| 40-60   | 120            |
| 60-80   | 100            |
| 80-100  | 70             |
| 100-120 | 50             |

38. (a) Explain Predictor-Corrector Milne's method.

- (b) Find  $y(0.3)$  for the differential equation  $\frac{dy}{dx} = x^2 + y^2 - 2$  satisfying  $y(-0.1) = 1.09$   
 $y(0) = 1, y(0.1) = 0.89, y(0.2) = 0.7605$

(2 × 13 = 26 Marks)

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