

19U501

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Name:

Reg. No:

FIFTH SEMESTER B.Sc. DEGREE EXAMINATION, NOVEMBER 2021

(CBCSS-UG)

CC19U MTS5 B05 - THEORY OF EQUATIONS AND ABSTRACT ALGEBRA

(Mathematics – Core Course)

(2019 Admission - Regular)

Time: 2 ½ Hours

Maximum: 80 Marks

Credit: 4

Section A

Answer *all* questions. Each question carries 2 marks.

1. What is the quotient obtained when $x^5 - 3x^2 + 6x - 1$ is divided by $x^2 + x + 1$?
2. What is the remainder obtained when $x^6 - x^5 + 5x + 3$ is divided by $x - 3$?
3. Write the Tylor's Formula for writing an n^{th} degree Polynomial $f(x)$ in powers of $(x - c)$
4. Write a cubic equation with roots 0, 1, 2
5. Find the sum and product of roots of $x^3 + 2x^2 + 3x + 2 = 0$.
6. Find the multiplicative inverse of 7 in Z_{15}
7. Write the addition table of Z_6
8. Find the number of generators of Z_{20}
9. Define a group. Give an example.
10. Check whether the following permutation is even or odd $(1,4,6,3)(2,3,5)$
11. Find the order of the permutation $(1,2,5,3)(3,4,5)$.
12. Define Zero divisors in a ring. Which are the zero divisors in Z_6 .
13. In $GL_2(\mathbb{R})$, find the order of $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$.
14. Let $\sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 4 & 1 & 2 & 5 \end{pmatrix}$, $\tau = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 1 & 4 & 2 & 5 & 3 \end{pmatrix}$, compute $\sigma\tau$.
15. Check whether the relation on \mathbb{R} , defined by $a \sim b$ if $a \geq b$ is an equivalence relation

(Ceiling: 25 marks)

Section B

Answer *all* questions. Each question carries 5 marks.

16. Solve $x^4 - 2x^3 + 6x^2 + 22x + 13 = 0$ having the root $2 + 3i$
17. Factorize into linear or quadratic factors $x^6 - 1$.
18. Solve $3x^3 - 16x^2 + 23x - 6 = 0$, if the product of two roots is 1.
19. Find an upper limit of positive roots of $2x^5 - 7x^4 - 5x^3 + 6x^2 + 3x - 10 = 0$.
20. Prove that the set of all even permutations in S_n is a group.
21. Draw the subgroup diagram of Z_{18} .

22. Let $S = \mathbb{R} - \{-1\}$, define $*$ on S by $a*b = a + b + ab$. Show that $(S, *)$ is a group.

23. Show that the set of all units of \mathbb{Z}_n is a group.

(Ceiling: 35 Marks)

Section C

Answer any *two* questions. Each question carries 10 marks.

24. Find the Integral roots of $x^6 + 3x^5 - 36x^4 - 45x^3 + 93x^2 + 132x + 140 = 0$.

25. Solve the cubic $3x^3 - 6x^2 - 2 = 0$.

26. Show that a sub group of a cyclic group is cyclic.

27. Show that set of all permutations on a set A is a group under permutation multiplication.

(2 × 10 = 20 Marks)
