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THIRD SEMESTER M.Sc. DEGREE EXAMINATION, DECEMBER 2015

(CUCSS)

Statistics

STA 3C 11—STOCHASTIC PROCESSES

(2010 Admission onwards)

me: Three Hours

Maximum: 36 Weightage

Part A

Answer all questions.

Each question carries 1 weightage.

- 1. Give an example of a stochastic process.
- 2. Write down the different classes of a stochastic process.
- 3. What is lack of memory in the disore case?
- 4. How can you write the one step transition probabilities?
- 5. When will you say that a process is stationary?
- 6. What is equilance class?
- 7. Define periodicity.
- 8. How will you find out the higher order transition probabilities?
- 9. Can a process remain in a transient class for ever?
- 10. Define stationary distribution.
- 11. What is offspring distribution?
- 12. Write down the central limit theorem for renewals.

 $(12 \times 1 = 12 \text{ weightage})$

Part B

Answer any **eight** questions. Each question carries 2 weightage.

- 13. What is a random walk?
- 14. Give an example of a recurrence chain.
- 15. Show that inter-occurrence time in a Poisson process is exponential.
- 16. What is a birth-death process?
- 17. Describe a queueing model.

Turn over

- 18. What is Little's formula?
- 19. Describe a renewal reward process.
- 20. What is Malthusian parameter?
- 21. What is Brownian motion?
- 22. Explain briefly a G/M/1 queue.
- 23. Describe a continuous time branching process.
- 24. Comment on inference on Markov chain.

 $(8 \times 2 = 16 \text{ weightage})$

Part C

Answer any **two** questions. Each question carries 4 weightage.

- 25. Find the mean and variance of a G.W. branching process.
- 26. State and prove elementary renewal theorem.
- 27. Establish a sufficient condition for a Markov chain to be transient.
- 28. Find the steady-state probability for an M/M/1 queue.

 $(2 \times 4 = 8 \text{ weightage})$