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Name.....Reg. No.....

# THIRD SEMESTER M.Sc. DEGREE EXAMINATION, DECEMBER 2015

(CUCSS)

Statistics

## STA 3C 12—TESTING OF STATISTICAL HYPOTHESIS

(2010 Admission onwards)

Time: Three Hours

Maximum: 36 Weightage

### Part A

Answer all questions.

Each question carries 1 weightage.

- 1. Distinguish between Parametric and Non-parametric tests.
- Define Power function and explain its use in testing.
- 3. When will you say that a family of distribution possesses MLR property?
- 4. Define test with Neymann structure.
- 5. Is UMP tests exists always? Justify your claim.
- 6. Show that Neyman-Pearson most powerful tests are unbiased.
- 7. Let  $X_1, X_2, ... X_n$  be a sample from a distribution function F and let  $F_n^*$  be the corresponding empirical distribution function. Show that  $D_n = \sup_n \left| F_n^*(x) F(x) \right|$  is distribution free.
- 8. Give the properties of Kendall's correlation coefficient tax.
- 9. Discuss  $\chi^2$ -test of independence of attributes.
- 10. Define O.C. function of SPRT.
- 11. Explain sequential estimation.
- 12. Justify the boundary points A and B of SPRT interms of the strength of the test.

 $(12 \times 1 = 12 \text{ weightage})$ 

### Part B

Answer any **eight** questions. Each question carries 2 weightage.

13. Find Neyman Pearson size  $\alpha$  test if  $H_0: \beta = 1$  vs  $H_1: \beta = \beta_1 (>1)$  based on a sample of size 1 from

$$f(x, \beta) = \beta x^{\beta-1}$$
  $0 < x < 1$   
= 0 elsewhere.

Turn over

14. Obtain the UMP test  $H_0: M \le M_0$  against  $H_1: M > M_0$  based on observations from hypergeometric

distribution with pmf 
$$P_M(X = x) = \frac{\binom{M}{x}\binom{N-M}{n-x}}{\binom{N}{n}} x = 0, 1, 2, \dots M.$$

- 15. Obtain the LR test for testing  $H_0: \mu = \mu_0 \ vs \ H_1: \mu \neq \mu_0$  based on observations from  $N\left(\mu, \sigma^2\right)$  of unknown.
- 16. Discuss briefly LMP and LMPU tests.
- 17. Derive the likelihood ratio test for testing  $H_0: \theta = 0$  vs  $H_1: \theta \neq 0$  in N  $(\theta, 1)$ . Further more show that this test is unbiased and consistent.
- 18. Explain Wilcoxon signed rank test.
- 19. Explain Mann-Whitney U-test for two sample problem.
- 20. Explain K-S two sample test.
- 21. Develop the SPRT for testing  $H_0: \theta = 3$  against  $H_1: \theta = 7$  based on observations from exp  $(\theta)$  wit strength (.05, .10).
- 22. Obtain the expressions for OC and ASN functions for testing  $H_0: \lambda = \lambda_0 \ vs \ H_1: \lambda = \lambda_1 \ based expressions from P(\lambda) with strength (\alpha, \beta).$
- 23. Describe Wald's SPRT. For aSPRT with stopping bounds A and B and strength  $(\alpha, \beta)$ , obtain th inequalities connecting the two.

 $(8 \times 2 = 16 \text{ weightage})$ 

#### Part C

Answer any **two** questions.

Each question carries 4 weightage.

- 24. Define UMP unbiased test. Show that there exists a UMP unbiased test for testing  $\mu = \mu_0$  again  $\mu \neq \mu_0$  based on observations from  $N(\mu, \sigma^2)$  with known  $\sigma^2$ .
- 25. What are similar region test? State and prove the necessary and sufficient conditions for similar region tests to have Neyman's structure.
- 26. (a) Explain ordinary sign test.
  - (b) Explain Median test.
- 27. Obtain the approximate expression of ASN function for testing  $H_0: \theta = \theta_0$  vs  $H_1: \theta = \theta_1$  strength  $(\alpha, \beta)$  based on observations from N  $(\theta, 1)$ . In particular obtain the expression of AS when  $\theta_0 = 2$  and  $\theta_1 = -2$ . Examine the nature of ASN function if  $\alpha = \beta$  by giving a rough sketch the curve.