# FIRST SEMESTER M.A. DEGREE EXAMINATION, FEBRUARY 2013

(CUCSS)

Economics

## Paper III—QUANTITATIVE TECHNIQUES—1

(2010 admissions)

Time: Three Hours

Maximum: 36 Weightage

## Part A

Answer all questions.

Each bunch of four questions carries weightage 1.

- A. Multiple Choice Questions:
  - 1 Gradient of a line joining points (2, 5) and (4, 13) is:
    - (a) 2.

(b) -2.

(c) 4.

- (d) -4.
- 2 When function Y =  $2x^2 + 3$  is differentiated from first principle,  $\frac{\Delta y}{\Delta x}$  is:
  - (a)  $4x^2$ .

(b)  $4x + 2\Delta x$ .

(c)  $4x^2 + 2\Delta x$ .

(d)  $\frac{4x^2}{2 \Lambda x}$ 

- 3 If  $y = \frac{1}{x^2}, \frac{dy}{dx}$  is:
  - (a)  $\frac{-2}{x^{-2}}$ .

(b)  $\frac{-2}{n^2}$ 

(c)  $\frac{-2}{x^3}$ .

- (d)  $\frac{-2}{r^{-3}}$ .
- 4 Determinant of a matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 5 \\ 1 & 2 & 3 \end{bmatrix}$  is :
  - (a) 0.

(b) 1

(c) 2.

(d) 5.

### B. Multiple Choice Questions:

- 5 Let A and B be two matrices. If AB = BA = I, then B is called:
  - (a) Cofactor of A.
- (b) Inverse of A.

(c) Minor of A.

- (d) · Adjoint of A.
- 6 For a straight line, Y-intercept is the point where:

- (c)  $y = x^2$ . (d)  $x = y^2$ .
- $7 \quad x^{-\frac{2}{3}} =$

- 8 A negatively sloped line moves:
  - (a) Upward.

- (b) Downward.
- (c) Horinzontally.
- (d) Vertically.
- C. Fill in the blanks:
  - 9 Given a supply function  $Q_s = -5 + 3p$  and a demand function  $Q_d = 10 2p$ , equilibrium
  - and ——— of a line. 10 The slope indicates the -
  - 11 In the income determination model  $Y = C_0 + bY_0 + I_0$ , b is called the —
  - 12 The joint occurrence of two or more simple events is called a -
- D. State True or False:
  - 13  ${}^{n}C_{r}$  is always equal to  ${}^{n}C_{n-r}$ .
  - 14 A difference equation is homogeneous if there is a constant term in the equation.
  - 15 For a demand function:

$$Q = 150 - 15 P$$
, when  $P = 4$  elasticity is  $\frac{2}{3}$ .

16 All indifference curves are convex to the origin.

 $(16 \times \frac{1}{4} = 4 \text{ weigh})$ 

Answer any ten questions, each not exceeding one page. Each bunch of four questions carries weightage 1.

17 Find the point of inflexion for the curve:

$$Y = x^3 - 3x^2 + 3x + 2.$$

- 18 What is partial differentiation? Write the partial derivatives of:
  - (a)  $Y = x^2 + 3xz 4z^2$ .
  - (b)  $Y = w^3 + w^2x + x^2z z^2$
- 19 What are the different types of matrices?
- 20 What is meant by rank of a matrix? Find the rank of matrix  $A = \begin{bmatrix} 2 & 5 & 1 \\ 3 & 2 & 4 \\ 1 & 4 & 2 \end{bmatrix}$ .
- 21 Solve the following system of equations using Cramer's rule:

$$6x_1 + 5x_2 = 49$$

$$3x_1 + 4x_2 = 32$$

22 Find the inverse of matrix:

$$A = \begin{bmatrix} 7 & 9 \\ 6 & 12 \end{bmatrix}.$$

23 What is a characteristic function? Find the characteristic roots of matrix:

$$A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}.$$

- 24 What is meant by economic optimisation? Optimise the function  $f(x) = 2x^3 30x^2 + 126x + 59$ .
- 25 State and prove the commutative property of matrix multiplication.
- What is implicit differentiation? Use implicit differentiation to find the derivative of the equation  $4x^2 y^3 = 97$ .
- 27 What is a random variable? Explain a probability distribution function.
- What do you mean by a binomial distribution? For a random sample from binomial distribution mean  $\bar{x} = 4$ , variance  $= \frac{12}{9}$ . Find n, p and q.

 $(10 \times 3.2 = 32 \text{ weightage})$