Time: 2 Hours

## FIRST SEMESTER B.C.A. DEGREE EXAMINATION, NOVEMBER 2019

(CBCSS UG)

## **CC19U BCA1 C01**

## MATHEMATICAL FOUNDATIONS FOR COMPUTER APPLICATIONS

(Mathematics -Complementary Course)

(2019 Admission Regular)

Maximum: 60 Marks Credit: 3

**Section A** – Short Answer type questions Each question carries 2 marks.

1. Find AB if 
$$A = \begin{bmatrix} 1 & 2 \\ 3 & -1 \end{bmatrix}$$
  $B = \begin{bmatrix} 1 & 3 \\ -1 & 0 \end{bmatrix}$ 

2. Find the determinant of the matrix 
$$\begin{bmatrix} 1 & 2 & 0 \\ 5 & 1 & 3 \\ -1 & 3 & 5 \end{bmatrix}$$

3. Find the eigen value of the matrix 
$$\begin{bmatrix} 8 & -4 \\ 2 & 2 \end{bmatrix}$$

4. Define limit of a function.

5. If 
$$\vec{a} = 2\vec{i} + \omega \vec{j} + 3\vec{k}$$
 and  $\vec{b} = \vec{i} - 2\vec{j} + 3\vec{k}$  are perpendicular. Find  $\omega$ 

6. Find the derivative of 
$$f(x) = x \sin x$$

7. Find the derivative of 
$$\frac{e^x}{1+\sin x}$$

8. Find 
$$\frac{dy}{dx}$$
 if  $y = \log \sqrt{1 + x^2}$ 

9. Evaluate 
$$\int x^6 + 5e^x + \frac{1}{x} dx$$

10. Evaluate 
$$\int \frac{x^2 + x + 1}{x} dx$$

11. Evaluate 
$$\int \frac{1}{x \log x} dx$$

12. Evaluate 
$$\int_0^1 \frac{dx}{1+x^2}$$

(Ceiling. 20 Marks)

**Section B** – Short Essay type questions Each question carries 5 marks.

13. Find the inverse of the matrix 
$$\begin{bmatrix} 2 & -1 & 1 \\ 3 & 1 & -5 \\ 1 & 1 & 1 \end{bmatrix}$$

14. If 
$$A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$$
 Show that  $A^2 - 3I = 2A$ 

15. If 
$$A = \begin{bmatrix} 0 & 6 & 7 \\ -6 & 0 & 8 \\ 7 & -8 & 0 \end{bmatrix}$$
  $B = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 2 \\ 1 & 2 & 0 \end{bmatrix}$   $C = \begin{bmatrix} 2 \\ -2 \\ 3 \end{bmatrix}$  Verify that  $(A + B)C = AC + BC$ 

16. If 
$$y = e^x \log x$$
 prove that  $\frac{dy}{dx} = y + \frac{e^x}{x}$ 

- 17. Using the quotient rule differentiate  $\frac{\sqrt{x} \cos x}{1+\sec x}$
- 18. Evaluate  $\int x e^{9x}$
- 19. Evaluate  $\int_0^{\frac{\pi}{2}} \frac{\sin x}{1 + \cos^2 x}$

(Ceiling. 30 Marks)

## **Section C** – Essay type questions

Answer any *one* question. The question carries 10 marks.

20. a) Find the rank of the matrix 
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 1 \\ 2 & 4 & 6 \end{bmatrix}$$

b) Find the solution of the linear equation by Gauss Jordan method

$$x + y + z = 0$$

$$x - 2v + 2z = 4$$

$$x + 2y - z = 2$$

21. a) Evaluate 
$$\int \frac{2x+1}{x^2+x+1} dx$$

b) Evaluate 
$$\int \frac{4x}{(x-2)(x-1)} dx$$

 $(1 \times 10 = 10 \text{ Marks})$ 

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